

# Structure in Neural Activity during Observed and Executed Movements Is Shared at the Neural Population Level, Not in Single Neurons

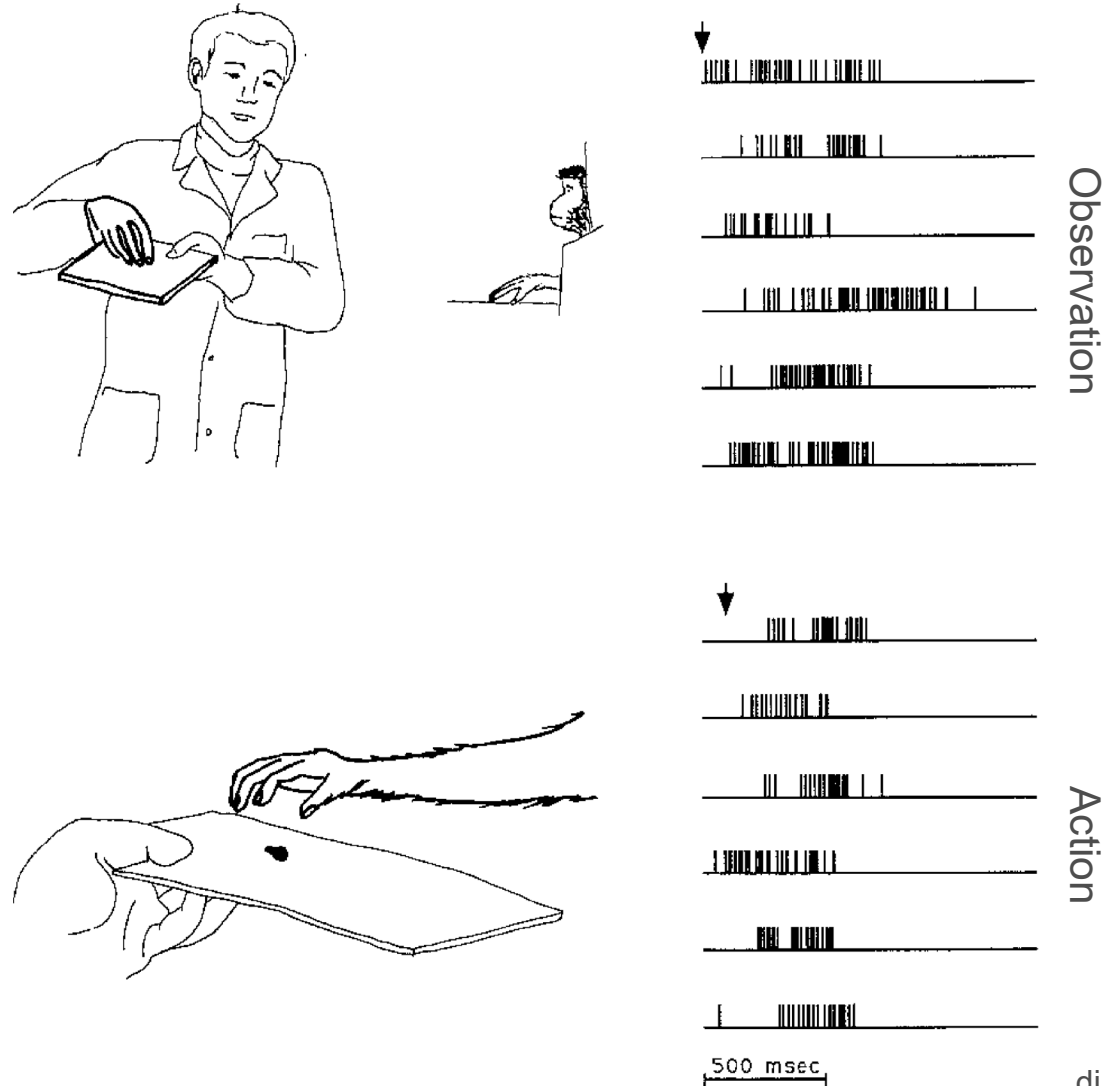
Jiang X., Saggar H., Ryu S.I., Shenoy K.V., and Kao J.C.

Presented by: James Goodman

NBL Journal Club

08.12.2020

# Mirror Neurons respond during action and observation



Observation

Action

di Pellegrino et al. 1992 *Exp. Br. Res.*

## Neuroscience Needs Behavior: Correcting a Reductionist Bias

or behavioral hypothesis is being tested per se. Thus, an interpretation is being mistaken for a result; namely, that the mirror neurons understand the other individual. Additional behavioral evidence that the participant understands the other individual is lacking. This tendency to ascribe psychological properties to

John W. Krakauer,<sup>1,\*</sup> Asif A. Ghazanfar,<sup>2</sup> Alex Gomez-Marín,<sup>3</sup> Malcolm A. MacIver,<sup>4</sup> and David Poeppel<sup>5,6</sup>

2017 *Neuron*

### Eight Problems for the Mirror Neuron Theory of Action Understanding in Monkeys and Humans

Gregory Hickok

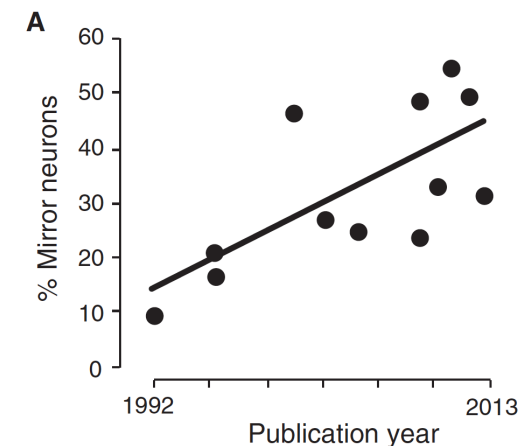
humans. The early hypothesis that these cells underlie action understanding is likewise an interesting and prima facie reasonable idea. However, despite its widespread acceptance, the proposal has never been adequately tested in monkeys, and in humans there is strong empirical evidence, in the form of physiological and neuropsychological (double) dissociations, against the claim.

2009 *J Cog. Neuro.*

### What We Know Currently about Mirror Neurons

J.M. Kilner and R.N. Lemon

2013 *Curr. Biol.*



"Mirror mechanism" may be better understood in neuronal state space

## Mirror Neuron Populations Represent Sequences of Behavioral Epochs During Both Execution and Observation

 Kevin A. Mazurek,<sup>1,2</sup>  Adam G. Rouse,<sup>2,3</sup> and  Marc H. Schieber<sup>1,2,3,4</sup>

2018 *J Neurosci.*

## Neurons in the Macaque Dorsal Premotor Cortex Respond to Execution and Observation of Actions

Vassilis Papadourakis<sup>1,2</sup> and Vassilis Raos<sup>1,2</sup>

2019 *Cereb. Cortex*

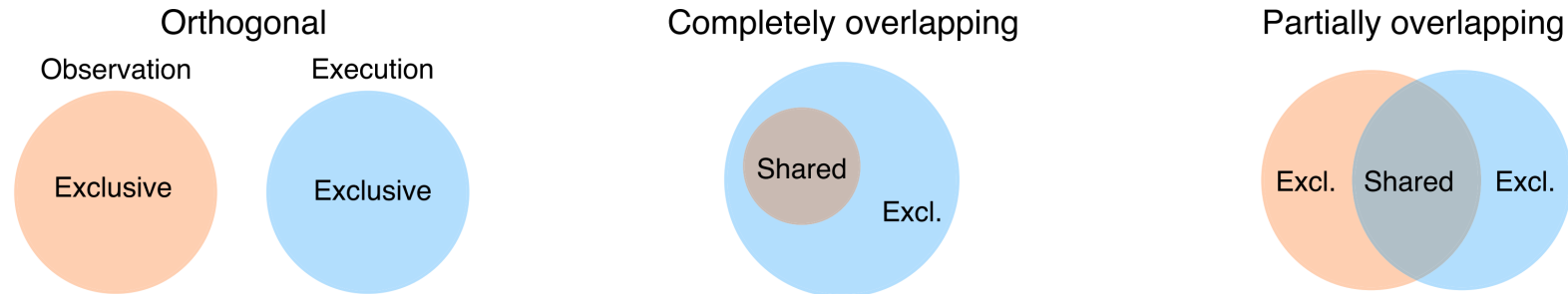
## Movement initiation and grasp representation in premotor and primary motor cortex mirror neurons

Steven Jack Jerjian<sup>1†</sup>, Maneesh Sahani<sup>2</sup>, Alexander Kraskov<sup>1\*</sup>

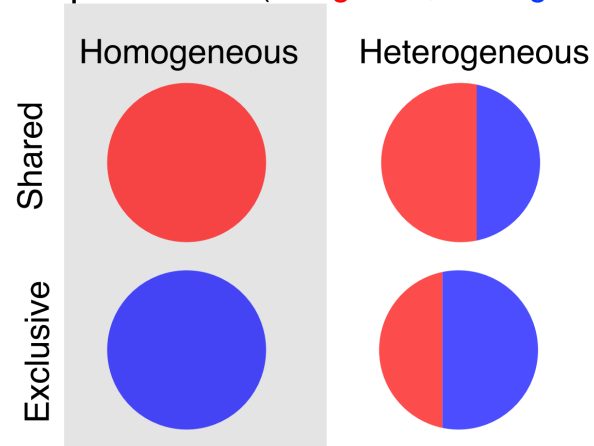
2020 *eLife*

# Hypotheses of population structure

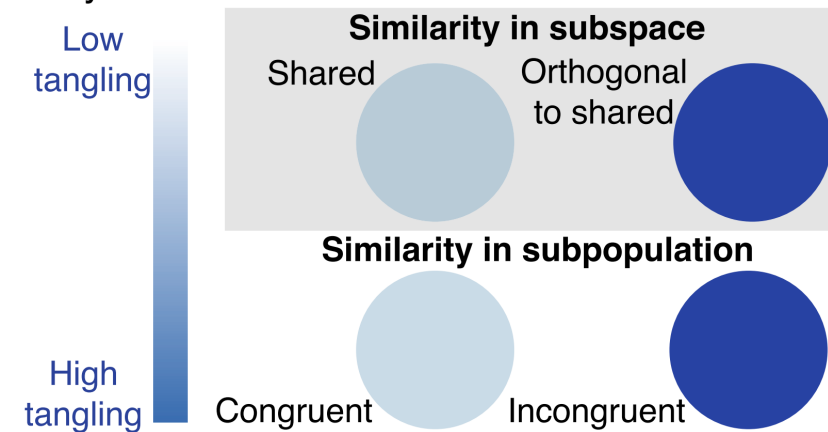
## A Subspace structure



## B Composition (Congruent, Incongruent)

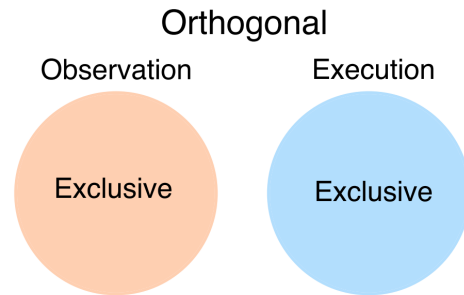


## C Dynamical structure

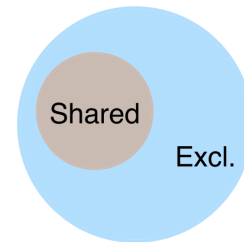


# A: Is observation activity orthogonal to, a subspace of, or partially overlapping with execution activity?

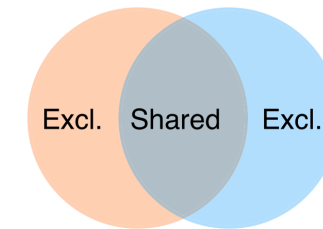
## A Subspace structure



## Completely overlapping

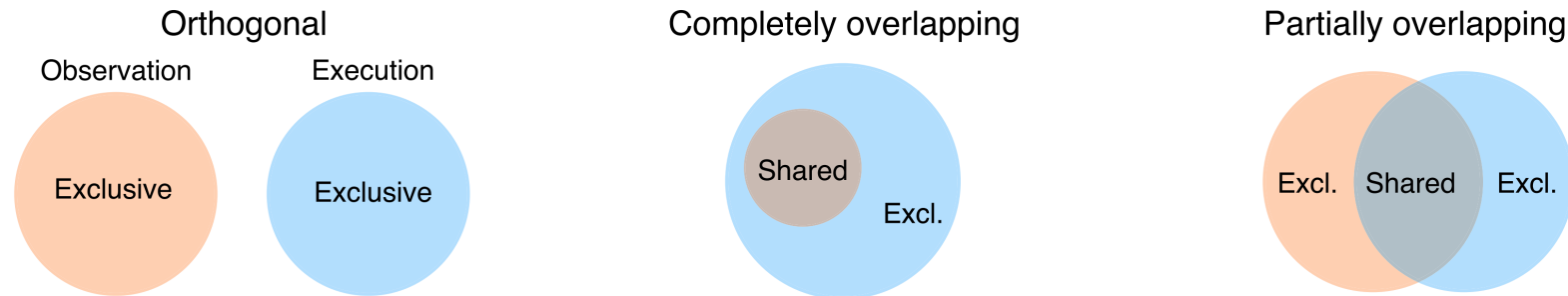


## Partially overlapping

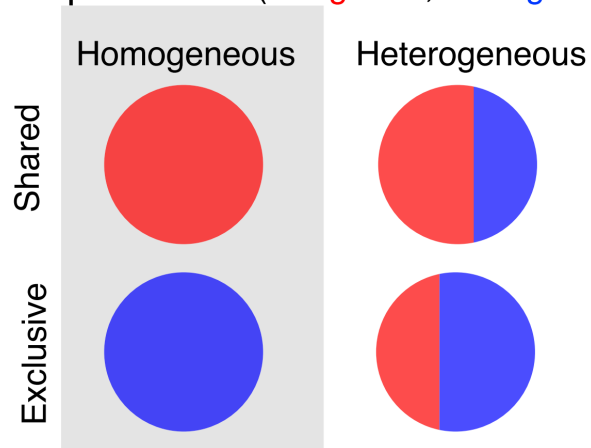


# B: Given an overlapping subspace, does it comprise a special set of "congruent" neurons? Or a heterogeneous mixture?

## A Subspace structure

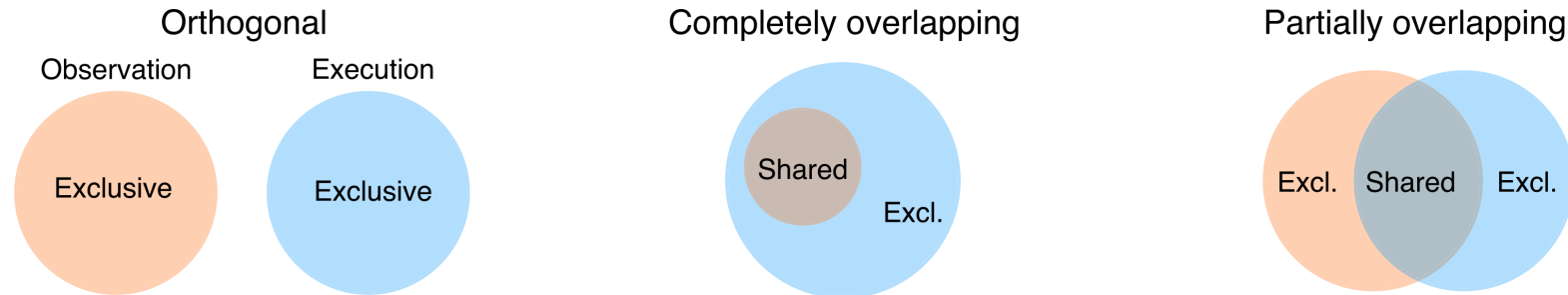


## B Composition (Congruent, Incongruent)

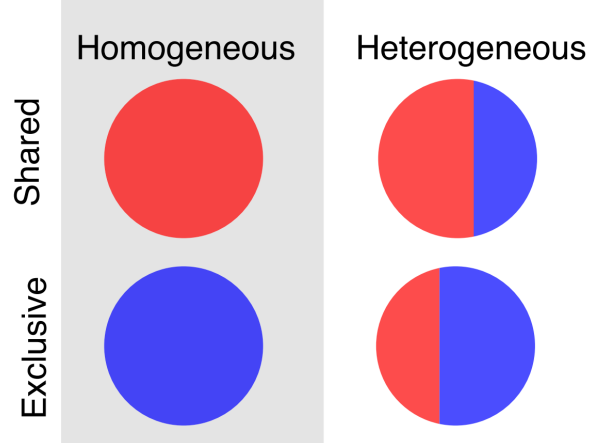


# C: Is dynamical structure preferentially preserved among "congruent" neurons? Or in a general shared subspace?

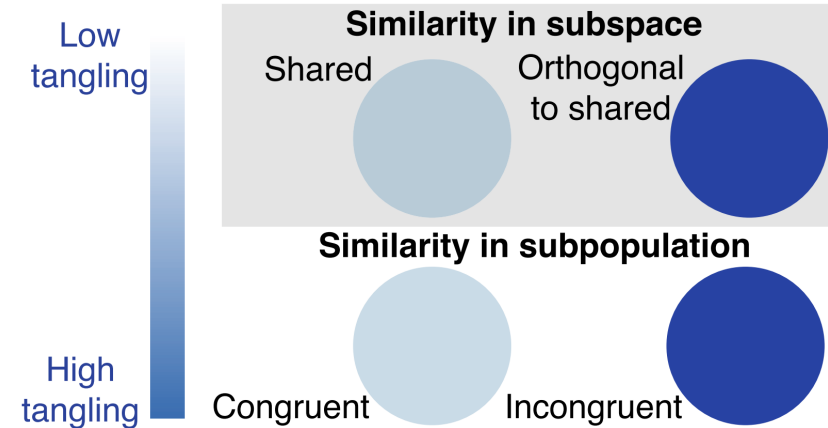
## A Subspace structure



## B Composition (Congruent, Incongruent)



## C Dynamical structure



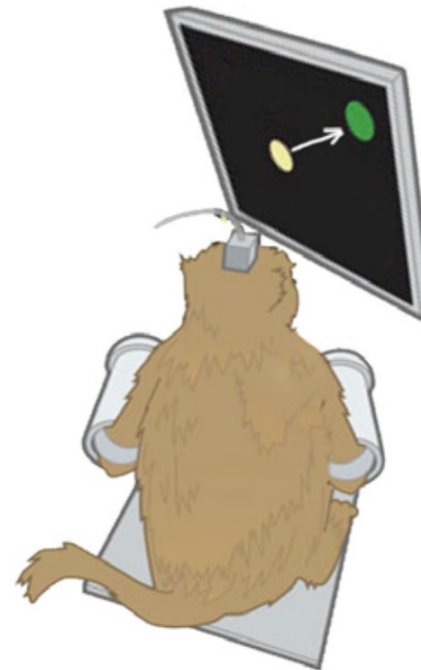


# Movement execution and observation experiments

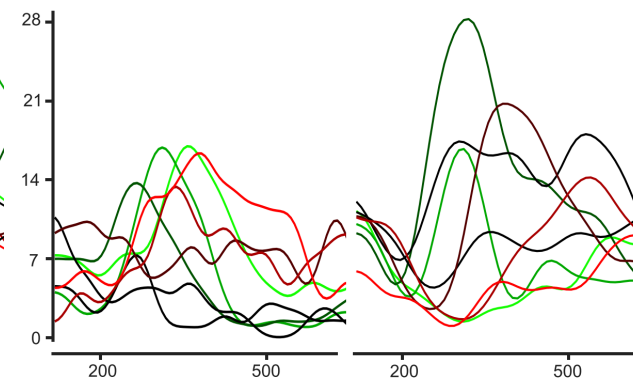
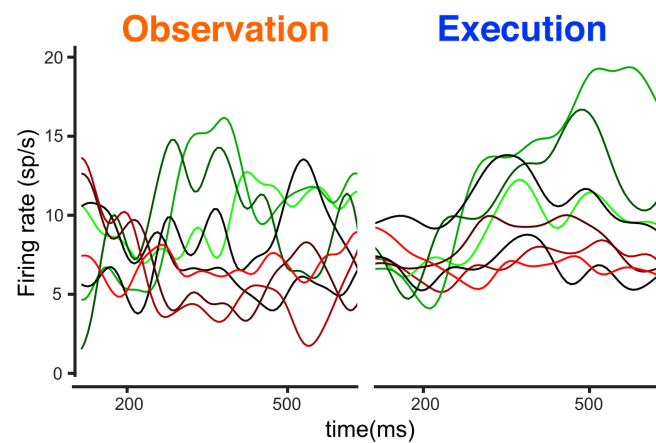
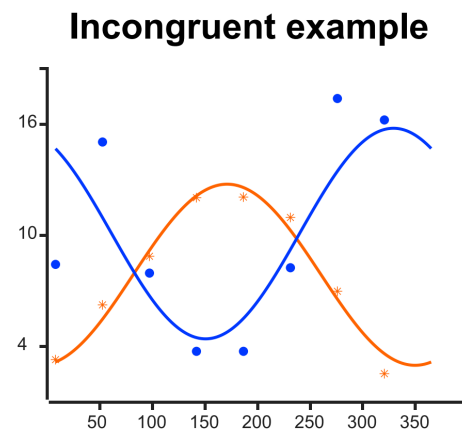
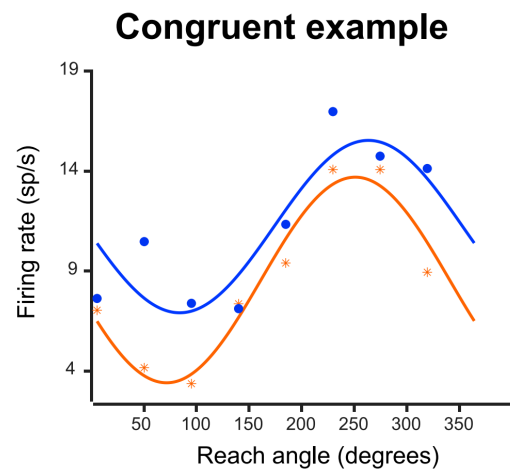
## Execution



## Observation



# Some neurons *could* be clustered into congruent and incongruent varieties...

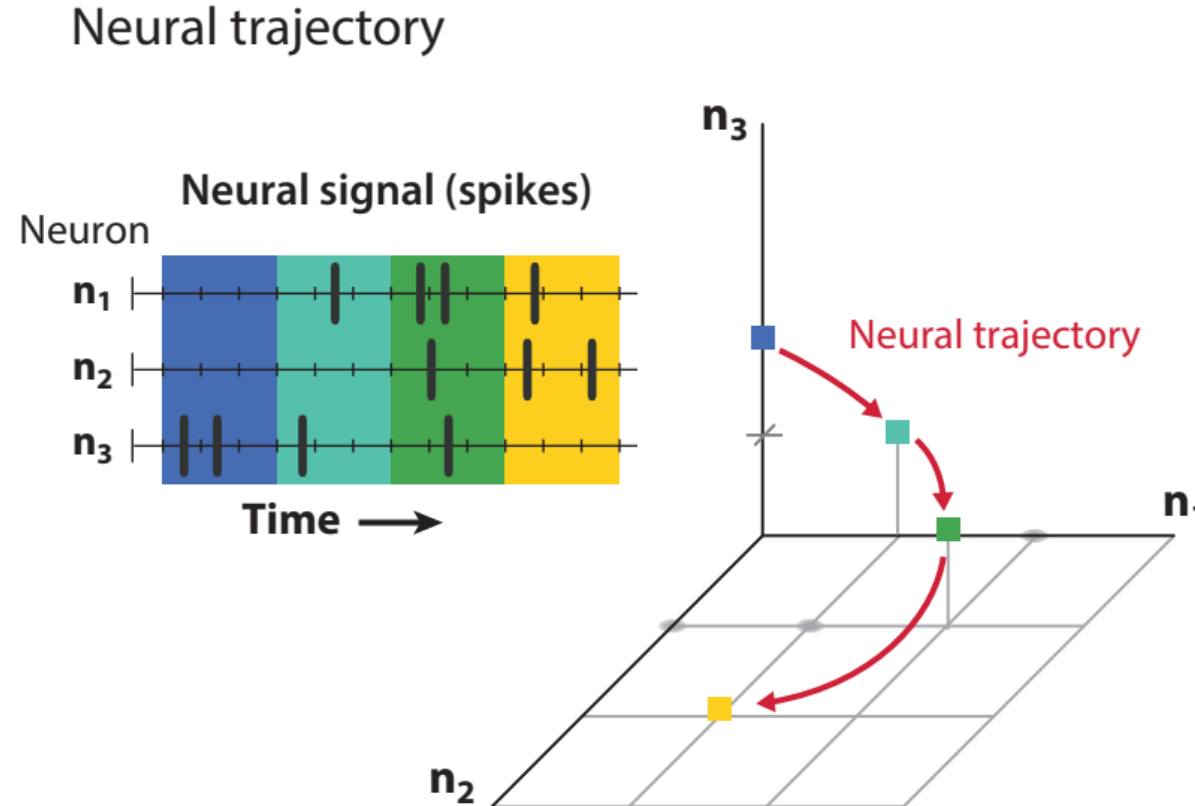


...but there's little evidence for distinct functional classes

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sition. To test this, we calculated each neuron's preference index for neuron  $i$  as  $B(i) = B_{\text{obs}}(i)/\bar{B}_{\text{obs}} - B_{\text{ex}}(i)/\bar{B}_{\text{ex}}$ , where  $B$  is tuning strength and  $\bar{B}$  is average tuning strength across all neurons (Elsayed et al., 2016). We then performed Hartigan's dip test on these preference indices to test if there was a bimodal distribution of observation versus execution-preferring neurons. We did not find that these neuron preference indices were bimodal ( $p = 0.974$  [0.978] in Monkey J [L]). Together, these results support the concept that a heterogeneous population is responsible for shared structure between observed and executed movements, rather than a subpopulation of neurons.

# Mixed, messy population justifies state space analysis!



Vyas et al. 2020 *Annu. Rev. Neurosci.*

$$A = \frac{\text{Tr}(\mathbf{Q}^T \mathbf{C} \mathbf{Q})}{\sum_{i=1}^d \lambda_i},$$

# Normalized variance captured in a subspace

**Q**: 10-D orthonormal basis

Can be:

- Top 10 Execution PCs
- Top 10 Observation PCs
- **Randomly-generated** from a uniform spherical distribution

$$A = \frac{\text{Tr}(\mathbf{Q}^T \mathbf{C} \mathbf{Q})}{\sum_{i=1}^d \lambda_i},$$

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**C**: Firing rate covariance matrix

Can be:

- **Observation** covariance
- **Execution** covariance

$$A = \frac{\text{Tr}(\mathbf{Q}^T \mathbf{C} \mathbf{Q})}{\sum_{i=1}^d \lambda_i},$$

$\lambda$ : Eigenvalue of  $\mathbf{C}$   
( $d = 10$  here)



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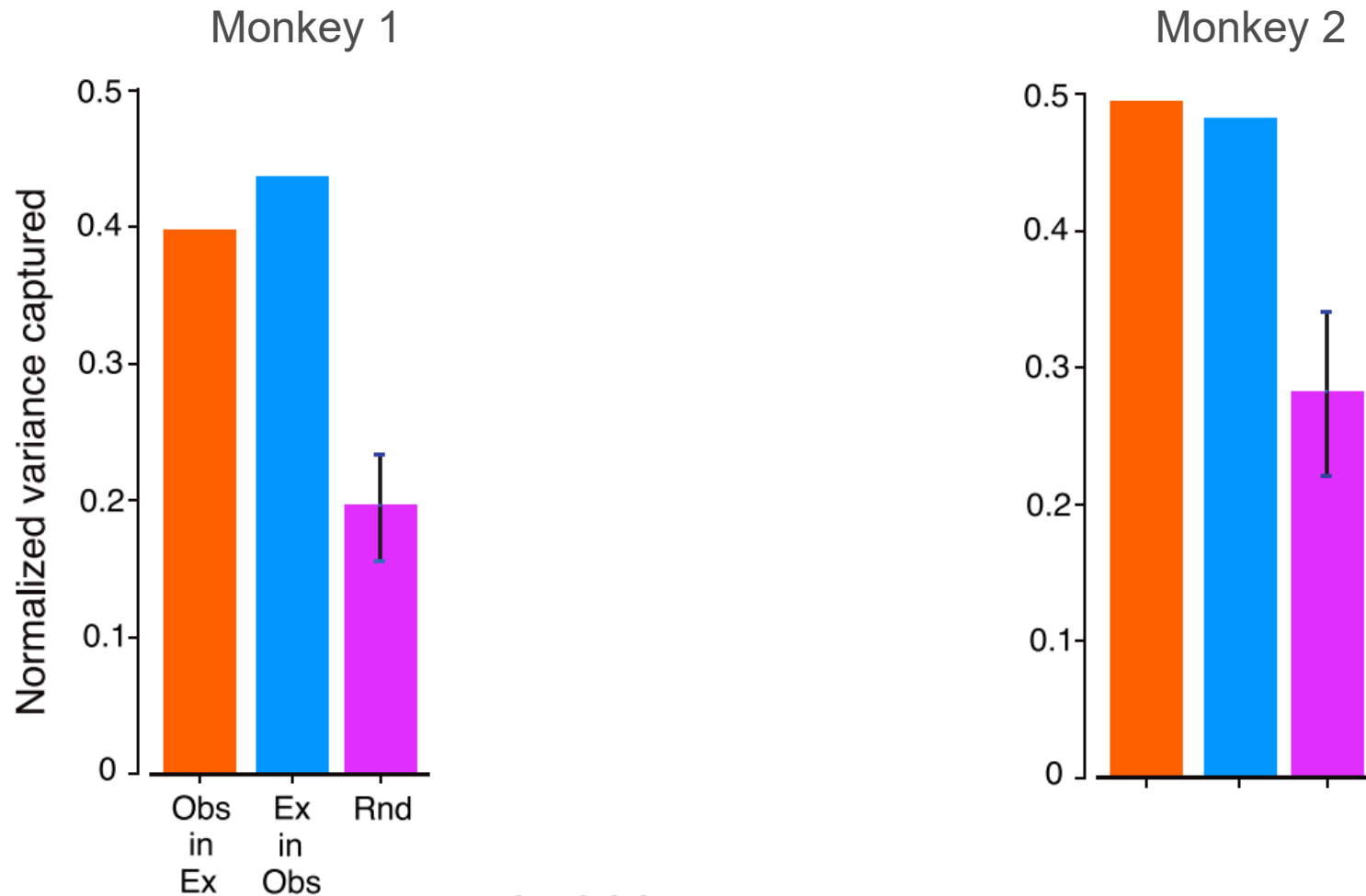
- **Observation** covariance
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$$A = \frac{\text{Tr}(\mathbf{Q}^T \mathbf{C} \mathbf{Q})}{\sum_{i=1}^d \lambda_i},$$

$\lambda$ : Eigenvalue of **C**

( $d = 10$  here)

# Observation and execution subspaces are not orthogonal



CROSS-projections

# Are we *sure* about that? Explicitly seeking orthogonal subspaces

$$\begin{aligned} & \text{maximize} \\ & \mathbf{Q} \in M_{d_{\text{Obs}} + d_{\text{Ex}}}(\mathbb{R}^N) \quad \frac{\text{Tr}\left(\mathbf{Q}_{\text{Orth-Obs}}^T \mathbf{C}_{\text{Obs}} \mathbf{Q}_{\text{Orth-Obs}}\right)}{\sum_{i=1}^{d_{\text{Obs}}} \lambda_i^{\text{Obs}}} + \frac{\text{Tr}\left(\mathbf{Q}_{\text{Orth-Ex}}^T \mathbf{C}_{\text{Ex}} \mathbf{Q}_{\text{Orth-Ex}}\right)}{\sum_{i=1}^{d_{\text{Ex}}} \lambda_i^{\text{Ex}}} \\ & \text{Subject to:} \quad \mathbf{Q}_{\text{Orth-Obs}}^T \mathbf{Q}_{\text{Orth-Ex}} = \mathbf{0}. \end{aligned}$$

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$$A = \frac{\text{Tr}(\mathbf{Q}^T \mathbf{C} \mathbf{Q})}{\sum_{i=1}^d \lambda_i},$$

(a) Observation on observation :  $\frac{\text{Tr}(\mathbf{Q}_{\text{Orth-Obs}}^T \mathbf{C}_{\text{Obs}} \mathbf{Q}_{\text{Orth-Obs}})}{\sum_{i=1}^{d_{\text{Obs}}} \lambda_i^{\text{Obs}}}$



(b) Observation on execution :  $\frac{\text{Tr}(\mathbf{Q}_{\text{Orth-Ex}}^T \mathbf{C}_{\text{Obs}} \mathbf{Q}_{\text{Orth-Ex}})}{\sum_{i=1}^{d_{\text{Ex}}} \lambda_i^{\text{Obs}}}$



(c) Execution on observation :  $\frac{\text{Tr}(\mathbf{Q}_{\text{Orth-Obs}}^T \mathbf{C}_{\text{Ex}} \mathbf{Q}_{\text{Orth-Obs}})}{\sum_{i=1}^{d_{\text{Obs}}} \lambda_i^{\text{Ex}}}$

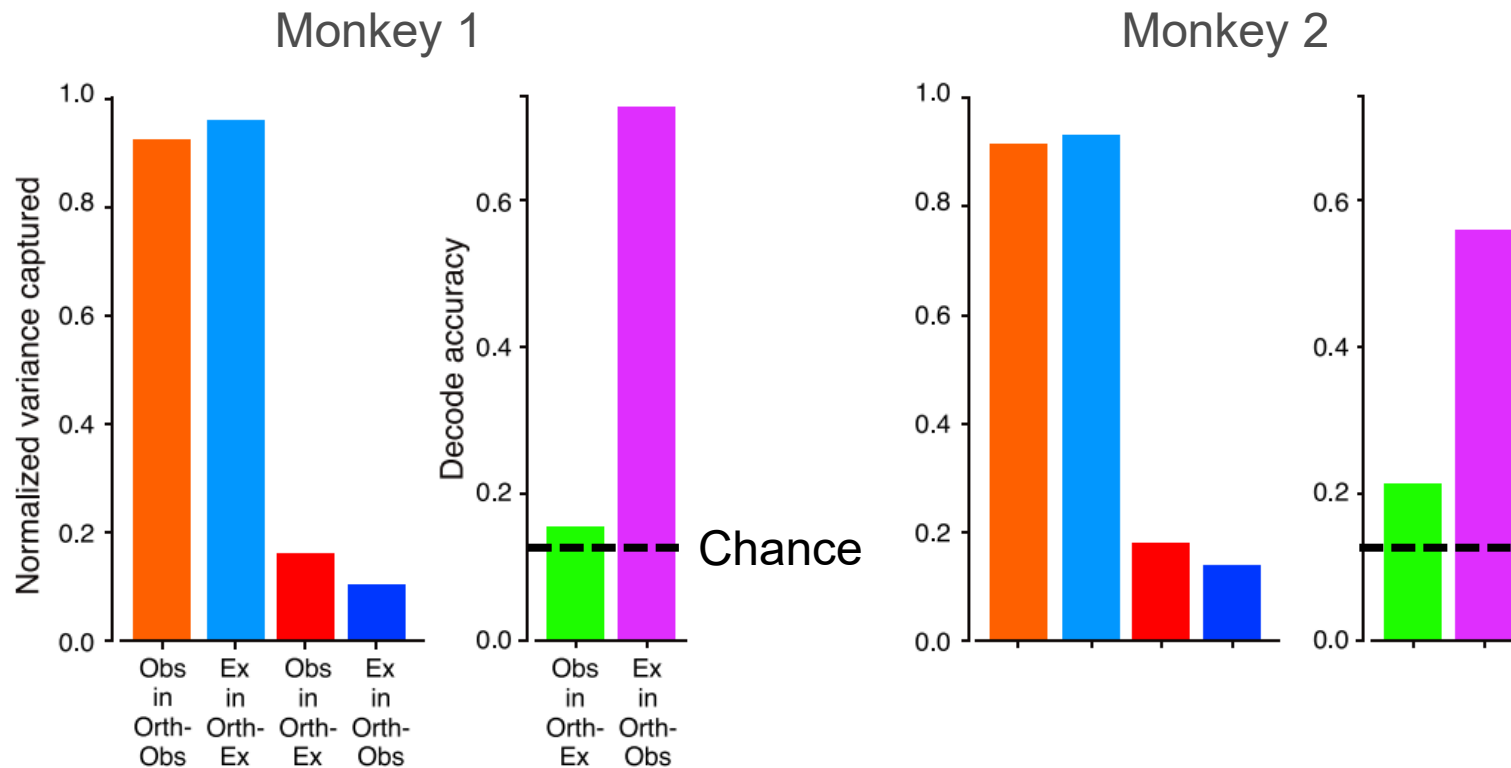
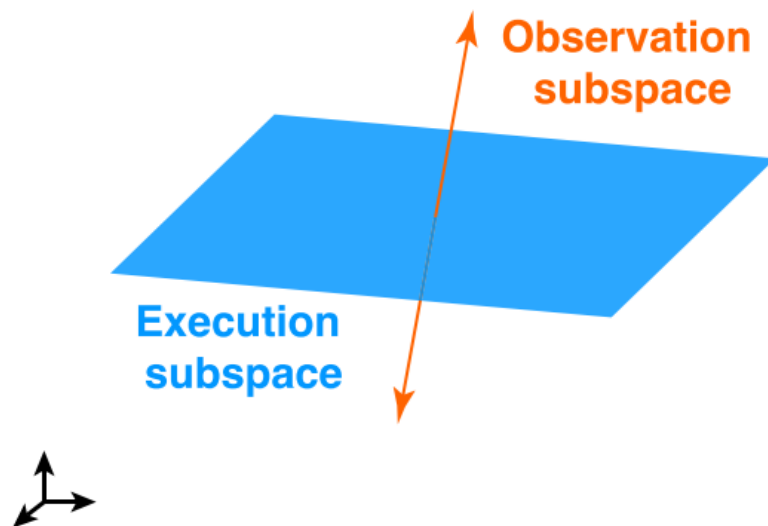


(d) Execution on execution :  $\frac{\text{Tr}(\mathbf{Q}_{\text{Orth-Ex}}^T \mathbf{C}_{\text{Ex}} \mathbf{Q}_{\text{Orth-Ex}})}{\sum_{i=1}^{d_{\text{Ex}}} \lambda_i^{\text{Ex}}}$

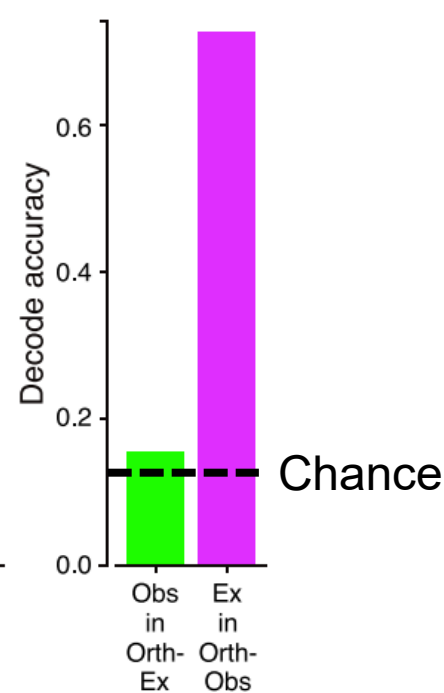
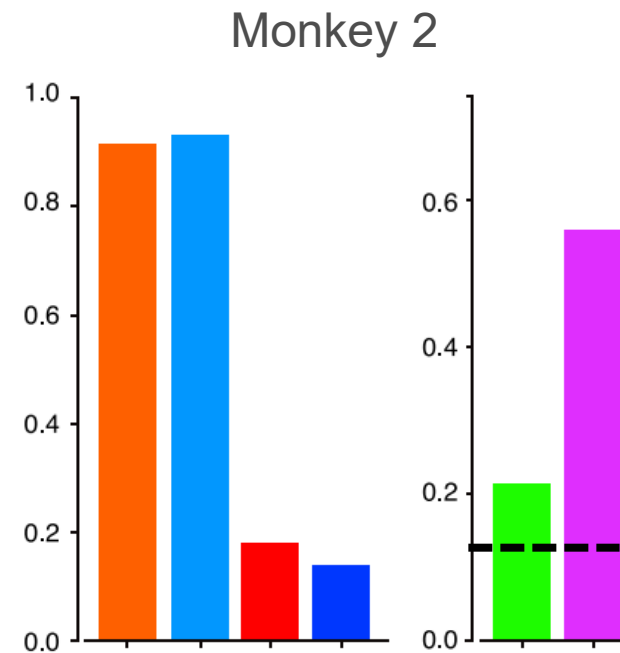
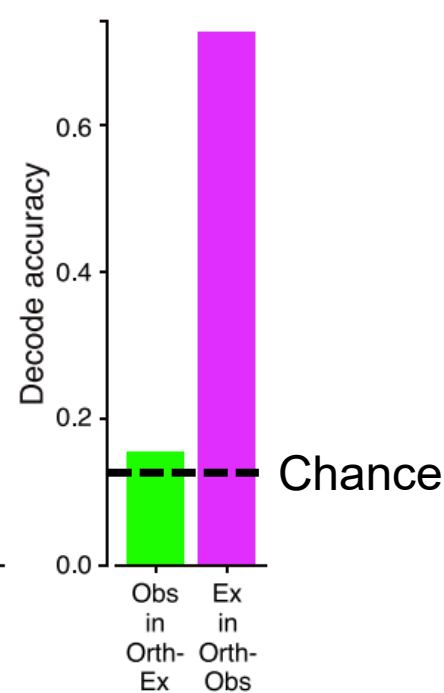
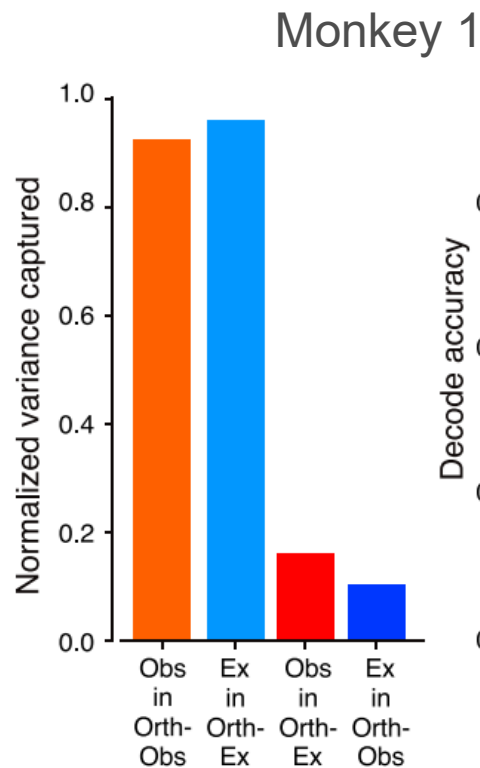
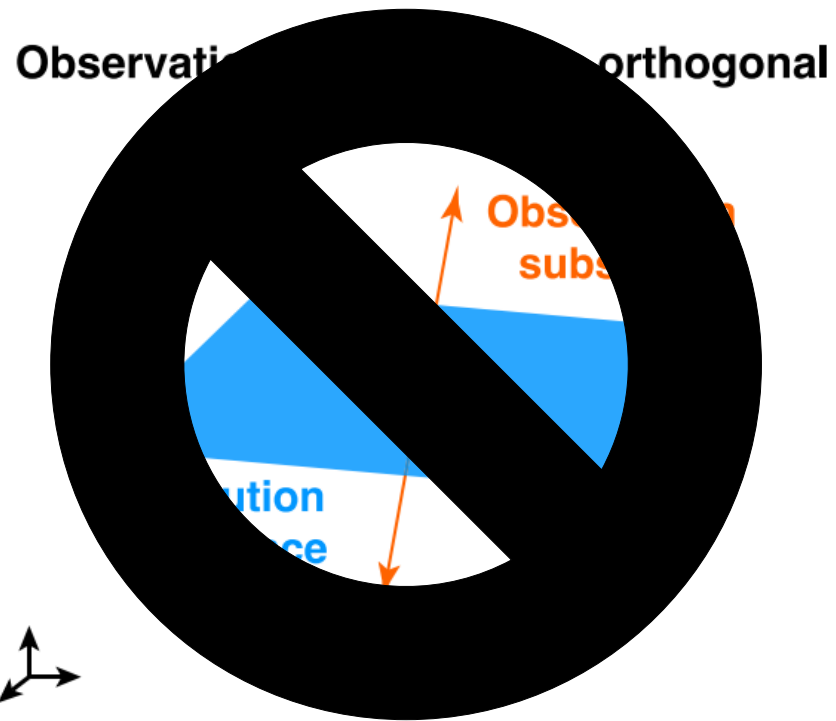


# "Orthogonal" subspaces contain nonzero, information-rich neural variance

## Observation and execution orthogonal



# "Orthogonal" subspaces contain nonzero, information-rich neural variance



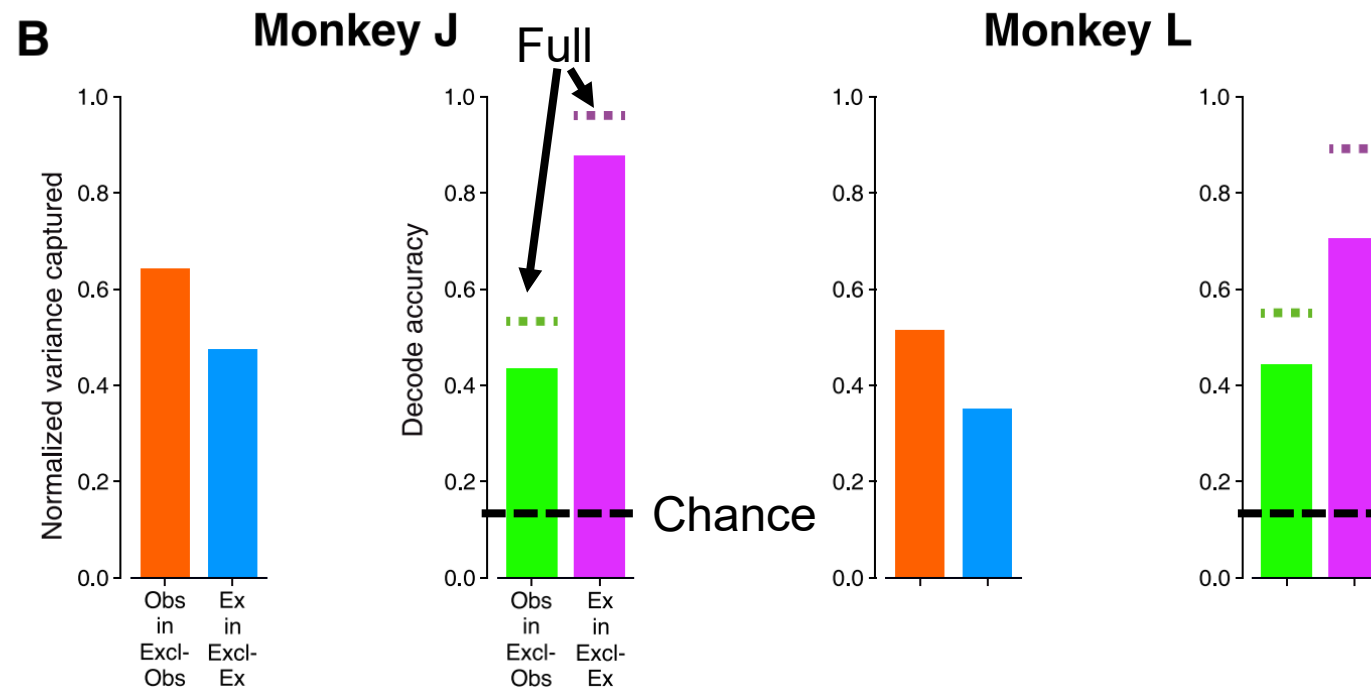
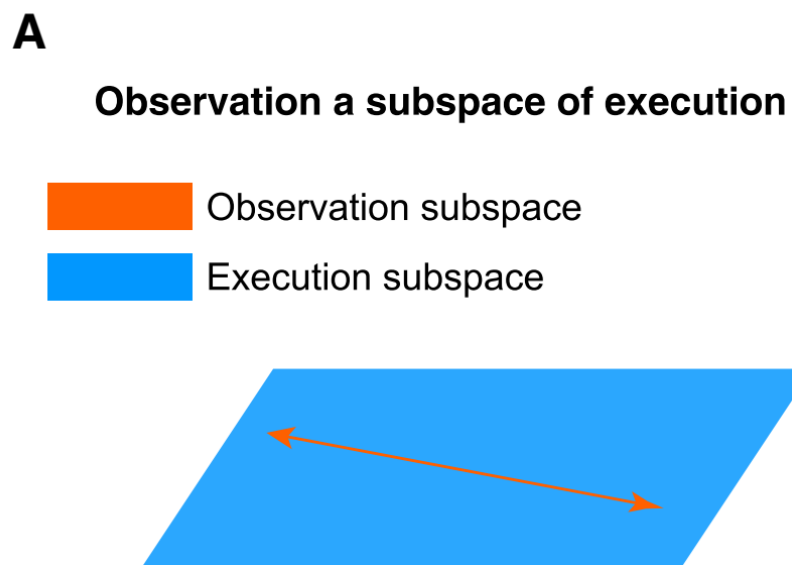
# Is observation activity a subset of execution activity? Seeking "exclusive" subspaces

$$\begin{aligned} & \text{maximize}_{\mathbf{Q}_{\text{Excl-Ex}} \in M_{d_{\text{Ex}}}(\mathbb{R}^N)} \frac{\text{Tr}\left(\mathbf{Q}_{\text{Excl-Ex}}^T \mathbf{C}_{\text{Ex}} \mathbf{Q}_{\text{Excl-Ex}}\right)}{\sum_{i=1}^{d_{\text{Ex}}} \lambda_i^{\text{Ex}}} \\ & \text{subject to} \frac{\text{Tr}\left(\mathbf{Q}_{\text{Excl-Ex}}^T \mathbf{C}_{\text{Obs}} \mathbf{Q}_{\text{Excl-Ex}}\right)}{\sum_{i=1}^{d_{\text{Ex}}} \lambda_i^{\text{Obs}}} \leq \nu \end{aligned}$$

(and vice-versa)



# Substantial "exclusive" subspaces show that observation activity is not a subset of execution activity

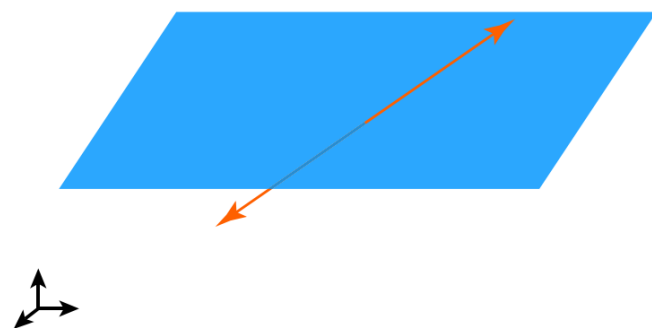


# Is the shared subspace meaningful? Seeking the "shared" subspace

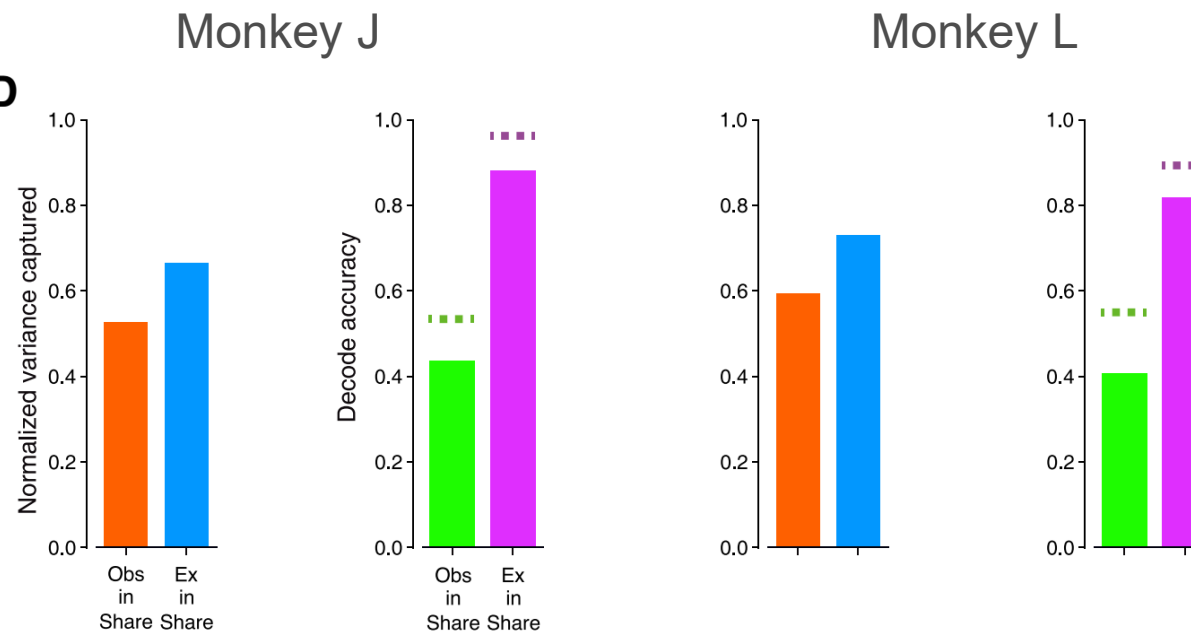
$$\begin{aligned} & \underset{\mathbf{Q}_{\text{Shared}} \in M_{d_{\text{Shared}}}(\mathbb{R}^N)}{\text{maximize}} && \frac{\text{Tr}\left(\mathbf{Q}_{\text{Shared}}^T \mathbf{C}_{\text{Ex}} \mathbf{Q}_{\text{Shared}}\right)}{\sum_{i=1}^{d_{\text{Shared}}} \lambda_i^{\text{Ex}}} + \frac{\text{Tr}\left(\mathbf{Q}_{\text{Shared}}^T \mathbf{C}_{\text{Obs}} \mathbf{Q}_{\text{Shared}}\right)}{\sum_{i=1}^{d_{\text{Shared}}} \lambda_i^{\text{Obs}}} \\ & \text{subject to} && \mathbf{Q}_{\text{Shared}} \perp \mathbf{Q}_{\text{Excl-Obs}} \\ & && \mathbf{Q}_{\text{Shared}} \perp \mathbf{Q}_{\text{Excl-Ex}} \end{aligned}$$

# The shared subspace captures substantial, information-rich variance

**C** Observation and execution share structure



**D**

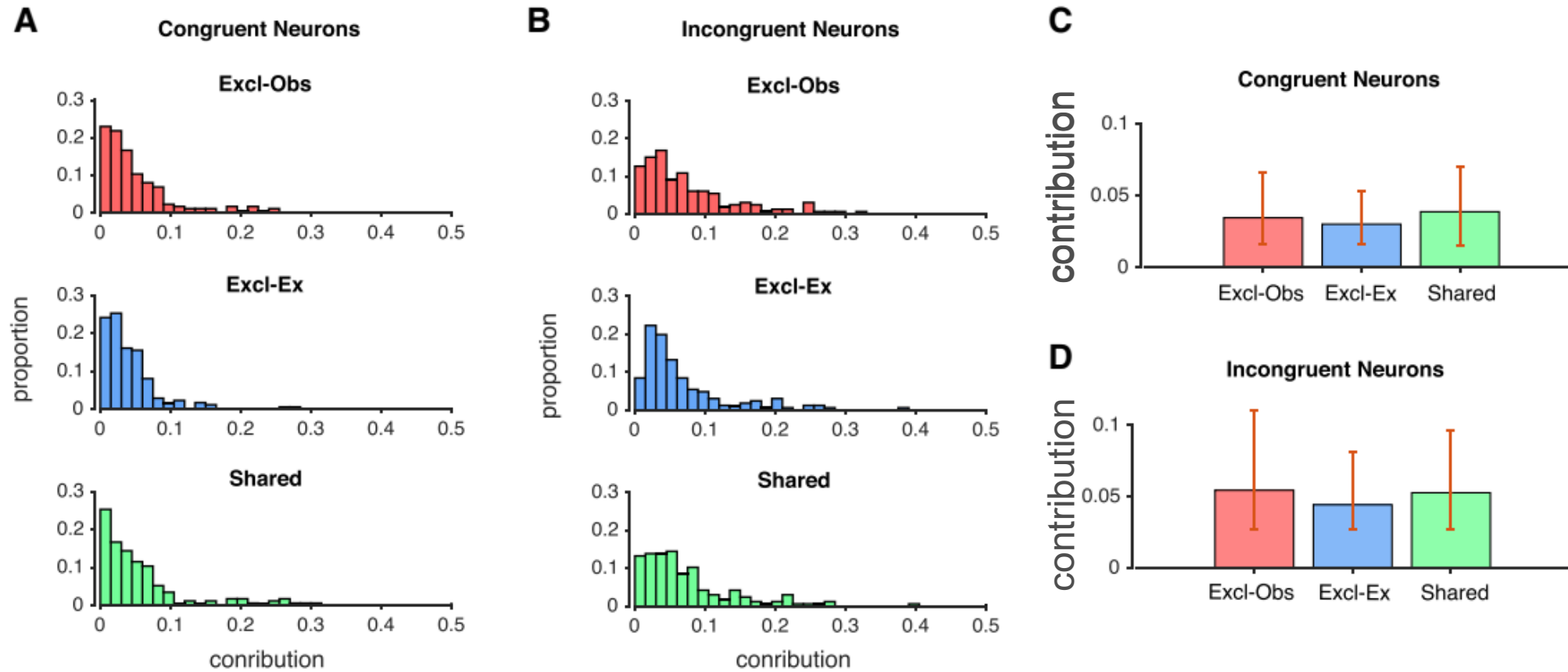


# How much does each neuron contribute to each subspace?

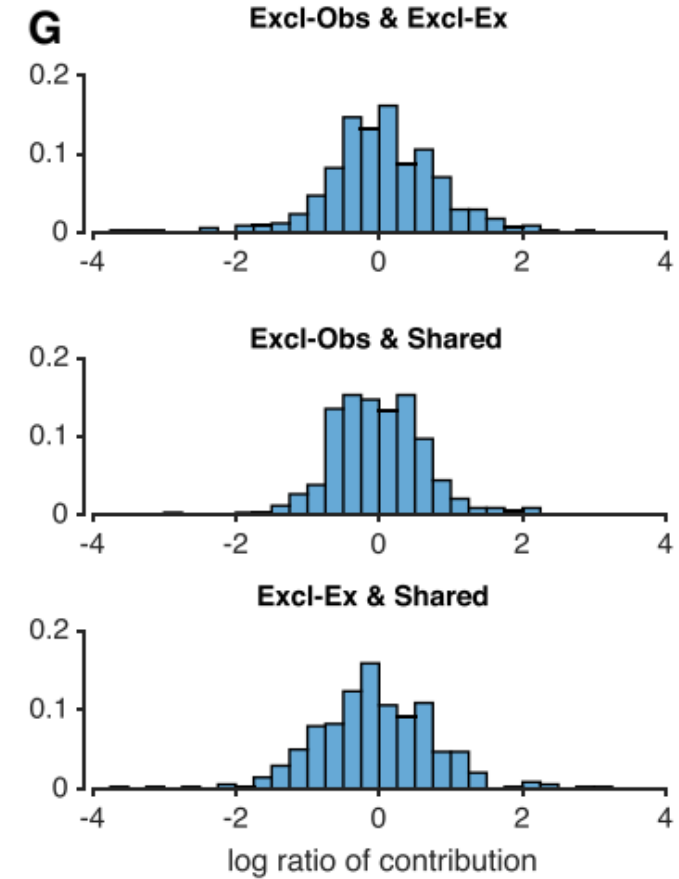
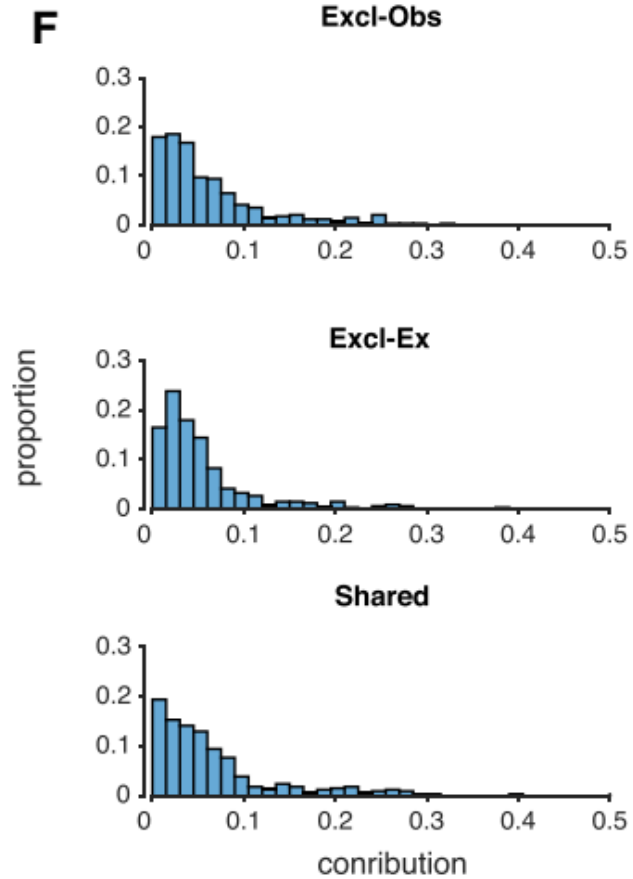
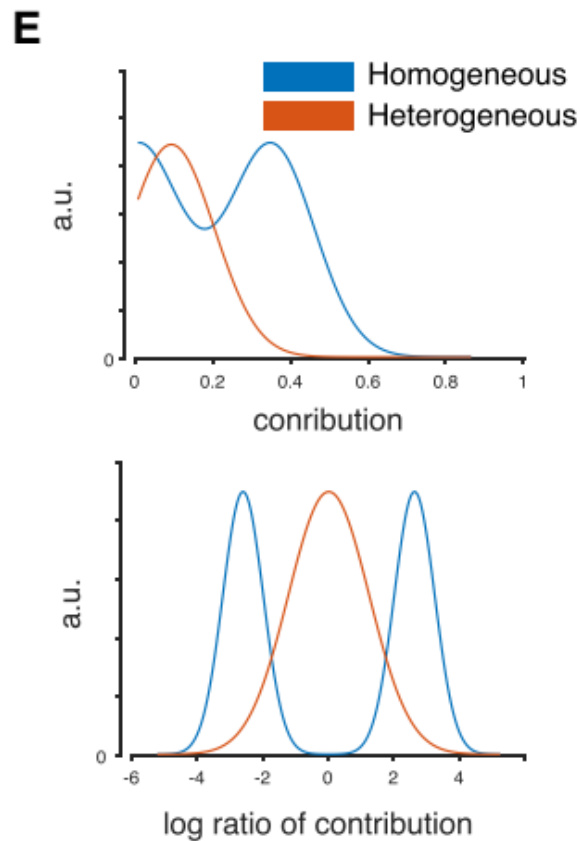
$$c_i = \sqrt{\frac{\text{Tr}(\mathbf{Q}^T \mathbf{X}_i \mathbf{X}_i^T \mathbf{Q})}{\text{Tr}(\mathbf{X}_i \mathbf{X}_i^T)}} \cdot FR = \sqrt{\frac{\text{Tr}(\mathbf{X}_i \mathbf{X}_i^T \mathbf{Q} \mathbf{Q}^T)}{\text{Tr}(\mathbf{X}_i \mathbf{X}_i^T)}} \cdot FR = \sqrt{\frac{\text{var}(x_i) \|\mathbf{w}_i\|^2}{\text{var}(x_i)}} \cdot FR = \|\mathbf{w}_i\| \cdot FR$$

where  $\text{var}(x_i)$  is neuron  $i$ 's total variance, and  $\|\mathbf{w}_i\|^2$  is the squared sum of  $\mathbf{Q}$ 's  $i^{\text{th}}$  row.

# The shared subspace is not merely a collection of congruent neurons

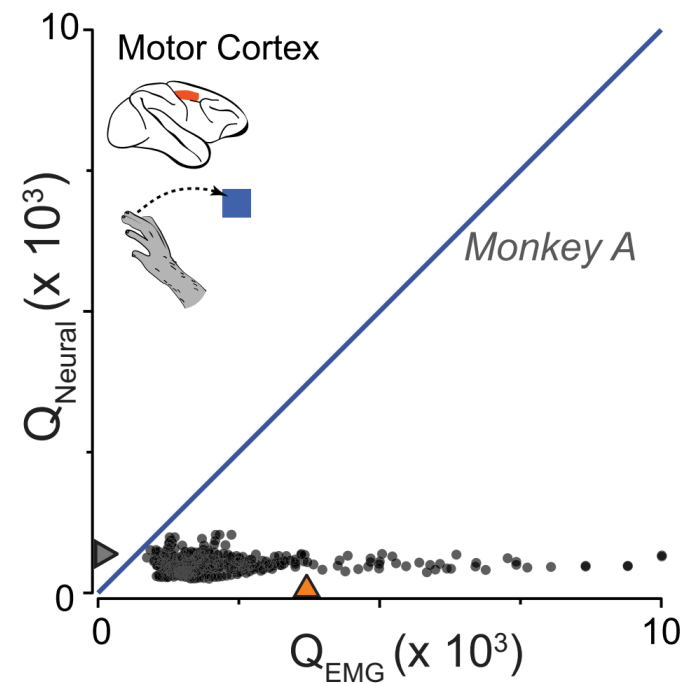
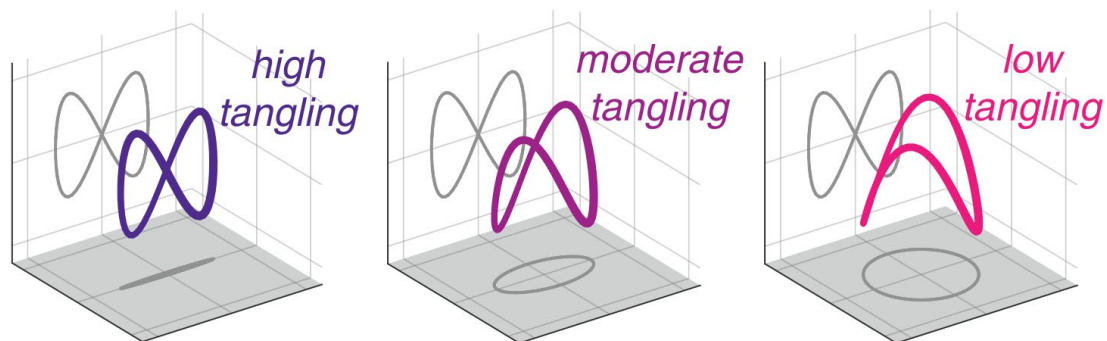


# No subspace defines a particular class of neurons – each subspace is a heterogeneous mix



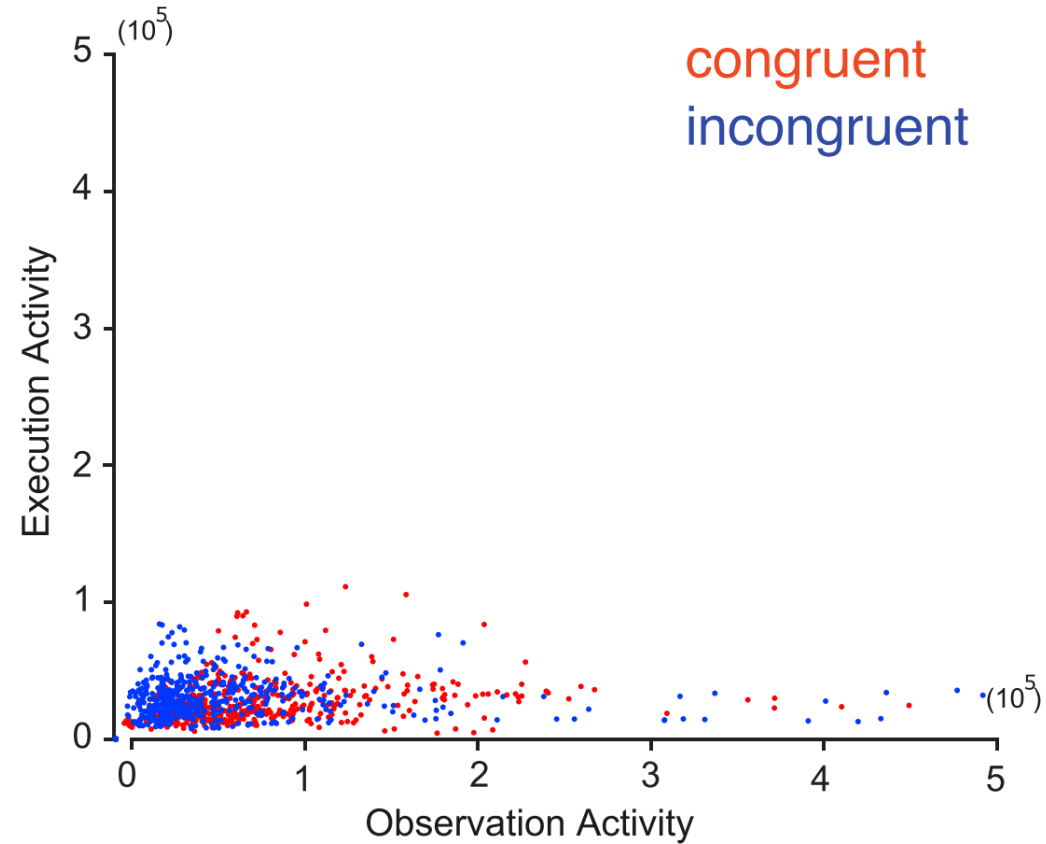
# Not just a representation: quantifying dynamical "tangling"

$$Q(t) = \max_{t'} \frac{\|\dot{\mathbf{x}}_t - \dot{\mathbf{x}}_{t'}\|^2}{\|\mathbf{x}_t - \mathbf{x}_{t'}\|^2 + \varepsilon},$$



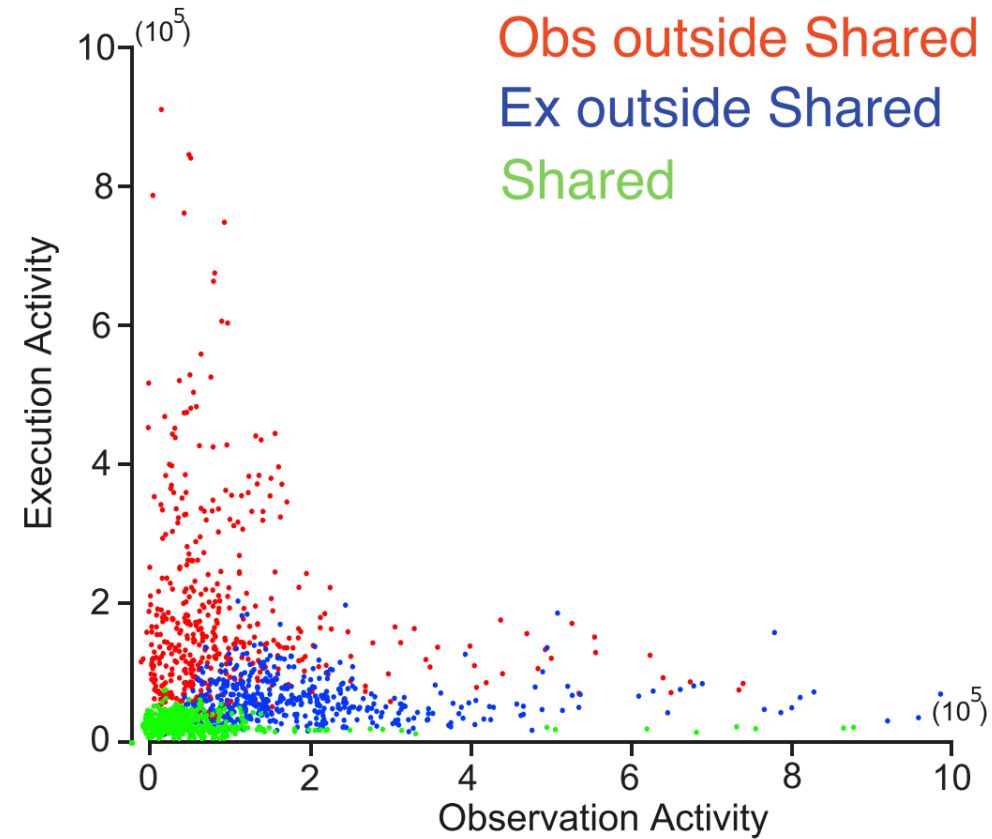
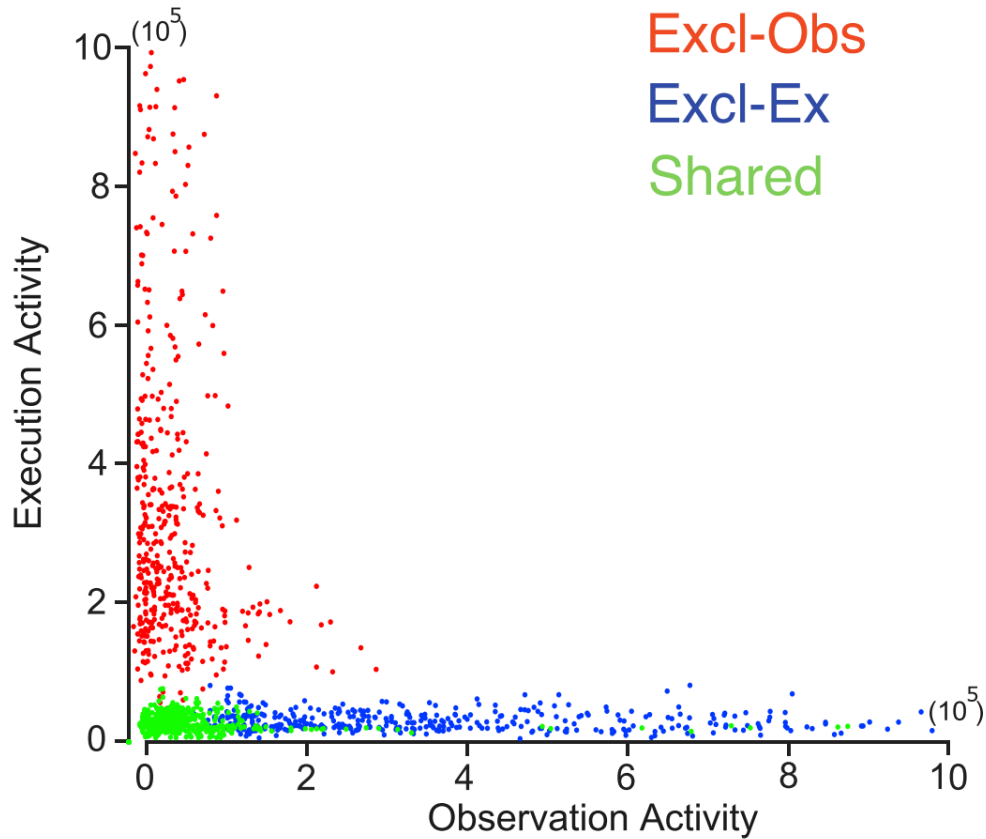
Russo et al. 2018 *Neuron*

# Congruent and incongruent neurons do not define dynamically distinct subspaces

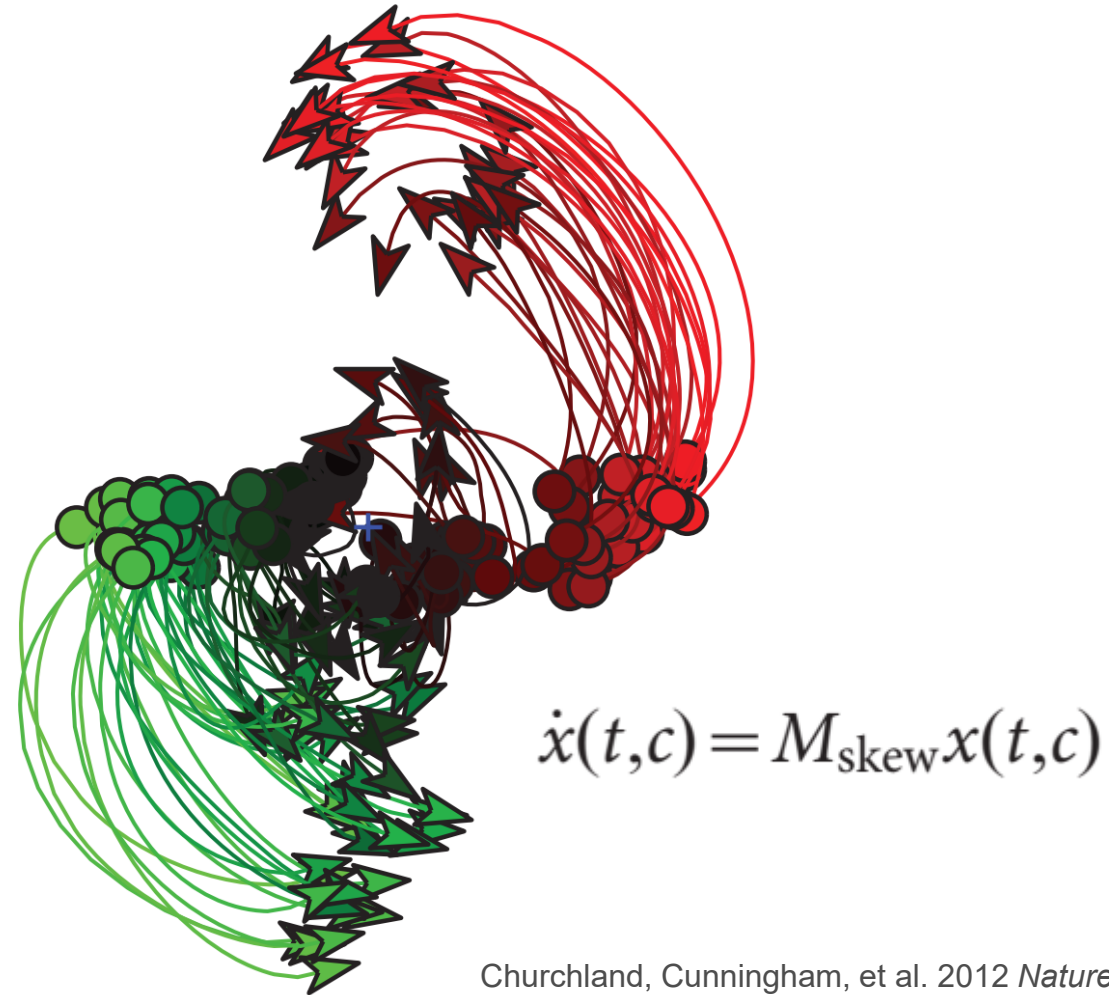




# Subspace decomposition reveals where observation activity exhibits low tangling



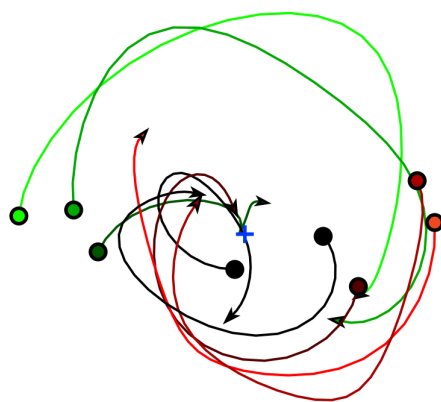
# What do these dynamics look like? Returning to jPCA



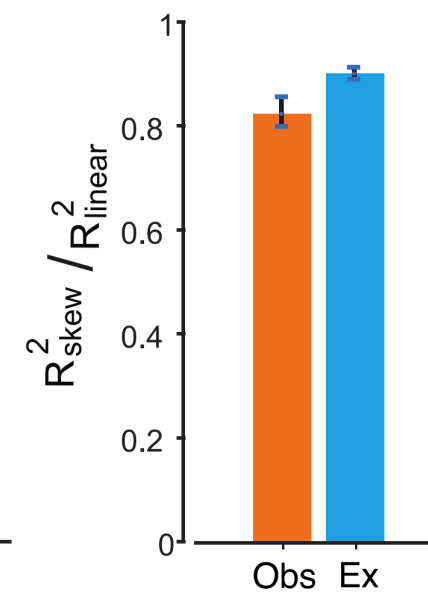
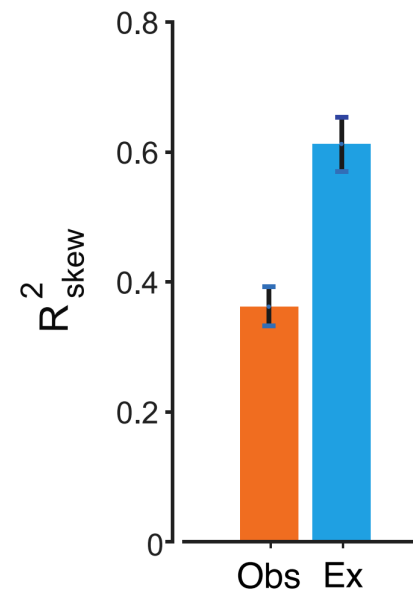
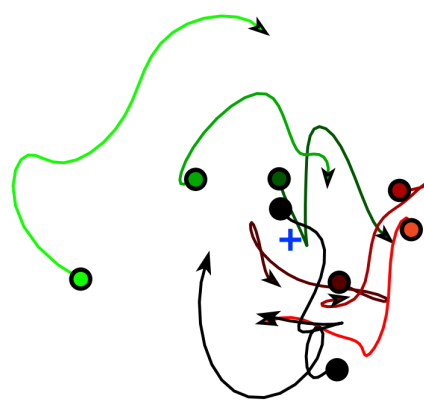
Churchland, Cunningham, et al. 2012 *Nature*

# Observation dynamics are weaker, but just as rotational, as execution dynamics

Execution



Observation



# Conclusions

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- There is no specific class of congruent mirror neurons
- Neural state spaces during action and observation are neither orthogonal nor totally overlapping
  - A "shared" subspace
  - Two "exclusive" subspaces
- Movement information is contained in both the shared and two exclusive subspaces
- Activity across all subspaces exhibits rotational dynamics, to the extent those subspaces are explored in a given context
- Overall, observation seems noisier than action
  - Less movement information
  - Weaker dynamics

# Caveats!

- No reporting of overall variance / firing rate / SNR within each condition
  - Only *differences* in baseline firing rate & modulation depth; both favor execution
  - How close to zero are we during observation?
- These animals have been trained on BCI cursor control
- Once more, PMd and M1 are pooled here
- No evidence that activity during observation is important for any kind of behavior